## Strategic Professional - Options

## Advanced Performance Management (APM)

## Wednesday 5 December 2018



Time allowed: 3 hours 15 minutes

This question paper is divided into two sections:
Section A - This ONE question is compulsory and MUST be attempted
Section B - BOTH questions are compulsory and MUST be attempted
Present Value and Annuity Tables are on pages 10 and 11.

Do NOT open this question paper until instructed by the supervisor.

This question paper must not be removed from the examination hall.

## Think Ahead

ACCA

The Association of Chartered Certified Accountants

## Section A - This ONE question is compulsory and MUST be attempted

1 Rezillos: Company information
Rezillos Engineering (Rezillos) is a listed company, manufacturing pumps and valves for use in the chemical industries. These highly engineered components must be integrated into Rezillos' customers' own plant and equipment. The company has grown significantly via acquisition in the last 20 years to become a worldwide business.

The overall objective of the company is 'to deliver sustainable growth in value to the shareholders by working in partnership with customers to deliver innovative and value-for-money solutions utilising the skills of the highly-trained workforce.'

The chief executive officer (CEO) has recognised that the company has been so focused on making acquisitions that it has not improved other aspects of management. He has asked you to produce a report for the board of Rezillos to cover a number of areas.

## Performance reporting system

The CEO would like an evaluation of the performance reporting system used at the strategic board level by Rezillos. The current performance report used for the annual review at board meetings is given as an example (Appendix 1).

## Customer survey

At the most recent round of meetings with stock market analysts, the board has been criticised about a customer survey whose results were announced at these meetings. The criticisms centred on the method of calculation, sampling and the disclosures in the press release. The board of Rezillos is concerned by the impact of this on their reputation in the market and needs to understand whether the criticism is justified. The press release and some further internal details about the method and the results of the customer survey are given in Appendix 2.

## Benchmarking proposal

Rezillos has three divisions based in its three countries of operation (Beeland, Teeland and Veeland). In order to drive forward the integration of the divisions, the CEO has decided that they should be benchmarked against each other. He is aware that this is not the only method of benchmarking and so, initially, wants you to provide an understanding of the different types of benchmarking and an evaluation of the usefulness of the proposed type of benchmarking for the divisions. Finally, he has supplied data in Appendix 3 to allow you to complete the benchmarking exercise and comment on the metrics used and the results.

It is now 1 December 20X8.

## Required:

## Write a report to the board of Rezillos to:

(a) Evaluate the performance reporting system as requested.
(b) Assess the analysts' criticisms of the customer survey results in Appendix 2.
(c) Respond to the CEO's request for work on:
(i) the method of divisional benchmarking proposed; and
(ii) benchmarking the three divisions.

Professional marks will be awarded for the format, style and structure of the discussion of your answer. (4 marks)

## Appendix 1

| Rezillos | Year to 30 September |  |  |  |  | Growth | Profit as a \% of revenue |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Beeland | Teeland | Veeland | Total | Total |  |  |  |
|  |  |  |  |  |  |  | Company | Industry average |
|  | 20x8 | $20 \times 8$ | $20 \times 8$ | 20x8 | 20x7 |  |  |  |
|  | \$m | \$m | \$m | \$m | \$m |  |  |  |
| Revenue | 738 | 2,030 | 923 | 3,691 | 3,504 | 5•34\% |  |  |
| Cost of sales | 497 | 1,391 | 601 | 2,489 | 2,363 |  |  |  |
| Gross profit | 241 | 639 | 322 | 1,202 | 1,141 |  | 32.6\% | 29•8\% |
| Other operating costs |  |  |  |  |  |  |  |  |
| Selling and distribution costs | 89 | 208 | 101 | 398 | 380 |  |  |  |
| Administration costs (note 1) | 74 | 171 | 83 | 328 | 321 |  |  |  |
| Total | 163 | 379 | 184 | 726 | 701 |  |  |  |
| Operating profit | 78 | 260 | 138 | 476 | 440 | 8•18\% | 12.9\% | 9.7\% |
| Finance costs |  |  |  | 88 | 88 |  |  |  |
| Group profit before tax |  |  |  | 388 | 352 |  | 10.5\% |  |
| Tax |  |  |  | 78 | 71 |  |  |  |
| Group profit after tax |  |  |  | 310 | 281 |  | 8.4\% |  |
| Return on capital employed ( | (ROCE) |  |  | 8.64\% |  |  |  |  |

## Note

1 Administration costs contain an allocation of product development costs to each division.

## Appendix 2

## Press release from Rezillos: Customer survey results

Rezillos has performed an extensive survey of its customer base and is proud to announce an average customer rating of $7 \cdot 0$ (out of 10 ). This bears positive comparison with a leading competitor of Rezillos who performed a survey last year scoring an average rating of 6.0.

The survey asked for a customer rating on a scale of 0 to 10 , where 10 was exceptional, 5 was good and 0 was unacceptable.

End of press release

## Extract from Rezillos internal document on calculation of customer rating

The survey was carried out by the staff at head office who sampled customers from all three divisions.

## Raw data

| Customer number | Rating | Account size $(\$ \mathrm{~m})$ | Division |
| :--- | :---: | :---: | :---: |
| 1 | 10 | $1 \cdot 5$ | Beeland |
| 2 | 9 | $3 \cdot 3$ | Beeland |
| 3 | 9 | $2 \cdot 1$ | Beeland |
| 4 | 6 | $6 \cdot 4$ | Beeland |
| 5 | 6 | $152 \cdot 0$ | Teeland |
| 6 | 6 | $11 \cdot 2$ | Beeland |
| 7 | 6 | $10 \cdot 5$ | Beeland |
| 8 | 6 | $74 \cdot 0$ | Veeland |
| 9 | 5 | $21 \cdot 0$ | Veeland |

## Other notes:

1 The company has 180 customers in total.
2 The customer number is an identification number for administrative purposes.
3 Each division has its own marketing and customer support function although product development is a head office function.

## Appendix 3 (all data is for 20X8 unless otherwise stated)

The benchmarking exercise is partly complete with the metrics requiring to be calculated identified by question marks.

|  | Beeland | Teeland | Veeland |
| :--- | ---: | ---: | ---: |
| Benchmarking metrics |  |  |  |
| Growth of market | $8 \cdot 5 \%$ | $3 \cdot 2 \%$ | $5 \cdot 0 \%$ |
| Revenue growth | $12 \cdot 5 \%$ | $3 \cdot 2 \%$ | $4 \cdot 8 \%$ |
| Operating margin | $10 \cdot 6 \%$ | $12 \cdot 8 \%$ | $15 \cdot 0 \%$ |
| Inventory days | 162 | 162 | $?$ |
| Order book growth | $5 \cdot 2 \%$ | $5 \cdot 3 \%$ | $?$ |
| Number of face-to-face interactions with division's top 10 key customers | 260 | 120 | 40 |
| Percentage of revenue from new products introduced in the last three years | $24 \cdot 9 \%$ | $29 \cdot 0 \%$ | $?$ |
| Reduction in incident rate | $3 \cdot 4 \%$ | $0 \cdot 0 \%$ | $?$ |
| Utilisation of learning and development programme | $1 \cdot 20$ | $1 \cdot 26$ | $?$ |

## Notes

1 The industry standard method of calculating incident rate is:
Incident rate $=$ number of incidents per year $\times 200,000 /$ number of employee labour hours paid
2 The company's employees work on average 40 hours per week for 50 weeks per year.
3 Utilisation of learning and development programme is measured by the number of training days per employee.
4 Key customers are designated by the divisional management.
5 A single inventory management system has been implemented across the whole company.
The following data has been collected to assist in the completion of the benchmarking exercise:
Veeland
Revenue from new products introduced in the last three years (\$m) 163
Cost of sales (\$m) 601
Inventory (\$m) 267
Number of incidents (20X8) 68
Number of incidents (20X7) 74
Number of employees (20X8) 6,600
Number of employees (20X7) 6,250
Order book (\$m) 20X8 932
Order book (\$m) 20X7 885
$\begin{array}{ll}\text { Number of training days } & 6,450\end{array}$

## Section B - BOTH questions are compulsory and MUST be attempted

## 2 Zones: Company information

Zones is an overnight parcel delivery business. Since it was founded by the current CEO, it has grown rapidly due to a boom in online shopping. It now operates 1,000 delivery vehicles of various sizes. Recently, financial performance and market share have deteriorated. Zones has had no clear corporate vision, an excessive focus on financial objectives and inadequate systems to measure and manage performance of the underlying processes driving its financial performance.

Business model
Zones' collection and delivery service uses delivery vehicles to transport parcels to and from local depots and individual addresses. Vehicles may also pick up parcels from the addresses to which they deliver. Each time the vehicle calls to pick up or deliver parcels is known as a stop, and the time of day for each stop is booked in advance. At the end of each day, vehicles, along with any parcels not delivered, return to the depot. Regardless of who pays for the service, Zones regards anyone to whom it delivers, or from whom it picks up parcels, as a customer. In the long term, the requirements of both of these groups for a competitively priced, reliable and flexible service will be similar.

## Performance improvement proposals

The CEO believes that reductions in customer satisfaction and flexibility, caused by a decline in operational performance, may have led to the recent deterioration in financial performance and market share. It has been suggested that Zones use the Lynch and Cross performance pyramid (Appendix 1) to reverse this deterioration, and three new measures for operational performance have been suggested in Appendix 2. The CEO has stated that Zones' corporate vision should be:
'To increase shareholder wealth by becoming the leading overnight parcel delivery business, providing quality, reliability and value for customers.'

It is also proposed to use the DMAIC (define, measure, analyse, improve and control) method to implement the six sigma methodology to improve the quality of delivery. Two measures have been defined in Appendix 3 which may help improve Zones' delivery performance.

## Required:

(a) Advise the CEO how the Lynch and Cross performance pyramid can help Zones achieve its corporate vision.
(b) Using the performance pyramid, evaluate the extent to which the suggested new measures in Appendix 2 can be used to measure and manage operational performance at Zones.
(9 marks)
(c) Advise whether the two measures defined in Appendix 3 are suitable for use in the DMAIC method to implement the six sigma methodology in order to improve delivery performance.

Appendix 1
Lynch and Cross performance pyramid


Appendix 2
Suggested new measures for operational performance

Measure
Vehicle utilisation

Fuel consumption
On-time stops

## Description

Average utilisation of all vehicle capacity. This is measured by taking the average of vehicle load as a percentage of capacity when the vehicle leaves the depot at the beginning of each day and the vehicle load as a percentage of capacity when the vehicle returns to the depot at the end of each day. Capacity is measured either according to the internal volume or the length of the vehicle, depending on the type of vehicle being used.

* Zones receives complaints from customers relating to deliveries not made on time. Of these, less than 0.0001\% relate to deliveries made within 30 minutes of the booked time.


## Appendix 3

## Suggested new measures for improving quality of delivery using the DMAIC methodology

## Measure

On-time stops
Failed deliveries

## Description

Percentage of stops made within 10 minutes of the booked time.
Percentage of deliveries which cannot be made due to the customer being unavailable to take the delivery, or by parcels being incorrectly addressed. Currently, $5 \%$ of deliveries are failed and have to be returned to the depot.

## 3 Sberry: Company information

Sberry manufactures products which have a short lifecycle due to technological obsolescence. It aims to keep each product in production for at least 18 months so that it can recover the high cost of product development and make an acceptable profit before the product becomes obsolete. Sberry has always manufactured its products in its home country of Deeland, from where all materials are also sourced.

## Sales opportunity in Kayland

An opportunity has been identified to export one of three newly developed products, Red, Blue and Green, to Kayland, due to citizens' increasing levels of income there. The rate of technological obsolescence is slower in Kayland than in Deeland. The estimated levels of demand, selling prices and costs of the three products are shown in Appendix 1.

Stakeholders' views on the risks of the Kayland opportunity
Three of Sberry's key stakeholder groups, employees, directors and shareholders, have been consulted for their views on the proposal to export to Kayland and, in particular, on which of the three newly developed products to export there.

The employees have a cautious approach to the proposal following the recent failure of another product launch. That product was withdrawn as it breached poorly understood safety regulations and a number of employees lost their jobs as a result.

The directors, all of whom are individually wealthy, have served on the board for many years and are keen to earn the large bonus which is currently offered solely on the total profit made by the new product over its lifecycle.

The shareholders neither avoid nor seek risk, but they are keen that the company considers the external environment in Kayland in order to maximise performance there, whichever of the products is chosen to be exported. They have asked for a PEST* analysis of the environment in Kayland to be produced. A first draft of this has indicated that the exchange rate between the Deeland dollar ( $D \$$ ) and the Kayland dollar ( $K \$$ ) is a key economic factor which may affect performance.
*Political, economic, socio-cultural and technological

## Required:

(a) Advise which of the three newly developed products each of the three key stakeholder groups would choose to export to Kayland based on their respective risk appetites.
(14 marks)
(b) Explain the problems of using the risk and uncertainty analysis techniques which you have used in part (a).
(c) Advise the shareholders how analysing the external environment in Kayland using a PEST analysis can help Sberry maximise its performance there. You are NOT required to produce a PEST analysis.

## Appendix 1

Estimated levels of demand, selling prices and costs of the three newly developed ${ }^{1}$ products

|  | Red | Blue | Green |
| :--- | ---: | ---: | ---: |
| Total demand $(\text { units })^{2}$ | 50,000 | 60,000 | 160,000 |
| Selling price $(\mathrm{K} \$)^{3}$ | 8.00 | 9.00 | 6.00 |
| Total unit cost $(D \$)^{4}$ | 2.40 | 3.00 | 2.50 |

Notes to the appendix
${ }^{1}$ Development costs are sunk costs and can be ignored.
2 The estimated product life of each of the three products is the same and the total demand is for the whole life of the product.
${ }^{3}$ The current exchange rate between the $D \$$ and the $K \$$ is $D \$ 1 \cdot 00=K \$ 2 \cdot 00$. Sberry's finance director has estimated that over the life of the product there is a $75 \%$ probability that the average exchange rate of the $D \$$ will strengthen by $10 \%$ against the $\mathrm{K} \$$, and a $25 \%$ probability that the average exchange rate of the $D \$$ will weaken by $10 \%$ against the K\$.
${ }^{4}$ At the current exchange rate, $50 \%$ of the total costs for each product is for materials which are imported from Kayland and invoiced in $\mathrm{K} \$$. There will be no opening or closing inventory, whichever of the three new products is chosen.

## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
Where $r=$ discount rate
$\mathrm{n}=$ number of periods until payment

Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\begin{array}{ll}
\text { Where } & r=\text { discount rate } \\
& n=\text { number of periods }
\end{array}
$$

Discount rate (r)
Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | $2 \cdot 941$ | $2 \cdot 884$ | $2 \cdot 829$ | $2 \cdot 775$ | $2 \cdot 723$ | $2 \cdot 673$ | $2 \cdot 624$ | 2.577 | $2 \cdot 531$ | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | $3 \cdot 465$ | $3 \cdot 387$ | $3 \cdot 312$ | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | 4.452 | 4.329 | $4 \cdot 212$ | 4.100 | 3.993 | 3.890 | 3.791 | 5 |
| 6 | $5 \cdot 795$ | 5.601 | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | $4 \cdot 355$ | 6 |
| 7 | $6 \cdot 728$ | 6.472 | 6.230 | 6.002 | 5.786 | $5 \cdot 582$ | 5.389 | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | 7.786 | 7.435 | 7.108 | $6 \cdot 802$ | 6.515 | $6 \cdot 247$ | 5.995 | $5 \cdot 759$ | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | 6.418 | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 368$ | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | $7 \cdot 139$ | $6 \cdot 805$ | $6 \cdot 495$ | 11 |
| 12 | $11 \cdot 255$ | 10.575 | 9.954 | $9 \cdot 385$ | 8.863 | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 134$ | $11 \cdot 348$ | $10 \cdot 635$ | 9.986 | $9 \cdot 394$ | 8.853 | 8.358 | 7.904 | 7.487 | $7 \cdot 103$ | 13 |
| 14 | 13.004 | $12 \cdot 106$ | 11.296 | 10.563 | 9.899 | 9.295 | $8 \cdot 745$ | $8 \cdot 244$ | $7 \cdot 786$ | $7 \cdot 367$ | 14 |
| 15 | 13.865 | $12 \cdot 849$ | 11.938 | $11 \cdot 118$ | $10 \cdot 380$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | $1 \cdot 605$ | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | $2 \cdot 402$ | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | 2.974 | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | 2.589 | 4 |
| 5 | $3 \cdot 696$ | 3.605 | $3 \cdot 517$ | 3.433 | $3 \cdot 352$ | 3.274 | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | 4.231 | $4 \cdot 111$ | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | $3 \cdot 326$ | 6 |
| 7 | $4 \cdot 712$ | 4.564 | $4 \cdot 423$ | $4 \cdot 288$ | $4 \cdot 160$ | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 | 7 |
| 8 | $5 \cdot 146$ | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | $5 \cdot 537$ | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | 4.772 | 4.607 | $4 \cdot 451$ | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | 5.889 | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | 4.659 | 4.494 | 4.339 | 4.192 | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | $5 \cdot 234$ | 5.029 | 4.836 | 4.656 | $4 \cdot 486$ | $4 \cdot 327$ | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | 4.988 | 4.793 | 4.611 | $4 \cdot 439$ | 12 |
| 13 | 6.750 | $6 \cdot 424$ | $6 \cdot 122$ | 5.842 | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | $6 \cdot 628$ | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | $4 \cdot 611$ | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | 5.847 | 5.575 | $5 \cdot 324$ | 5.092 | 4.876 | $4 \cdot 675$ | 15 |

## End of Question Paper

